## National Curriculum: Progression in Mathematics

## Early Years

## Nursery

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| Counting | $\bullet$ |
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| Numbers | $\bullet$ Fa |
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- Recite numbers past 5.
- Say one number name for each item in order: 1 , 2, 3, 4, 5. . Know that the last number reached when counting a small set of objects tells you how many there are in total ('cardinal principle')

| Numbers | - Fast recognition of up to 3 objects, without having to <br> count them individually ('subitising'). <br> - Show 'finger numbers' up to 5. <br> - Link numerals and amounts: for example, showing the |
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| Foundation | ELG |
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| - Count objects, actions and sounds. <br> - Count beyond ten. | - Verbally count beyond 20, recognising the pattern of the counting system. |
| - Subitise. <br> - Link the number symbol (numeral) with its cardinal number value. <br> - Compare numbers. | - Subitise (recognising quantities without counting) up to 5 . <br> - Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity. |
| - Understand the 'one more than/one less than' <br> relationship between consecutive numbers. <br> - Explore the composition of numbers to 10. | - Have a deep understanding of numbers to 10 , including the composition of each number. |
| - Automatically recall number bonds for numbers 0-10. <br> - Subitise. <br> - Link the number symbol (numeral) with its cardinal number value. | - Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10 , including double facts. <br> - Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed evenly. |
| - Compare length, weight and capacity. |  |


| Shape | - Talk about and explore 2D and 3D shapes (for <br> example, <br> circles, rectangles, triangles and cuboids) using <br> informal <br> and mathematical language: 'sides', 'corners', <br> 'straight','flat', 'round'. <br> •Select shapes appropriately: flat surfaces for a <br> building, a triangular pattern for a roof, etc. <br> - Combine shapes to make new ones - an arch, a <br> bigger triangle, etc. | Select, rotate and manipulate shapes in order to develop <br> spatial reasoning skills. |  |
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| Position and <br> direction | •Understand position through words alone - for <br> example, "The bag is under the table," - with no <br> pointing <br> $\bullet$ Describe a familiar route. <br> - Discuss routes and locations, using words like 'in front <br> of' and 'behind'. <br> - Talk about and identify the patterns around them. For <br> example, stripes on clothes, designs on rugs and <br> wallpaper. Use informal language like 'pointy', 'spotty', <br> 'blobs', etc. <br> •Extend and create ABAB patterns - stick, leaf, stick, <br> leaf. <br> - Notice and correct an error in a repeating pattern. | • Draw information from a simple map. <br> •Continue, copy and create repeating patterns. |  |

## Lower Phase

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Number - Place
Value
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## Year 1

-count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number (1NPV-1)
-count, read and write numbers to 100 in numerals; count in multiples of twos, fives and tens (1NF-2)
-given a number, identify one more and one less -identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least
-read and write numbers from 1 to 20 in numerals and words.

## Year 2

## Year 3

-count in steps of 2, 3, and 5 from 0 , and in tens from any number, forward and backward
-recognise the place value of each digit in a two-digit number (tens, ones)
-identify, represent and estimate numbers using different representations, including the number line
-compose and decompose two-digit numbers using standard and nonstandard partitioning (representing number links)
-compare and order numbers from 0 up to 100; use <, > and = signs
-read and write numbers to at least 100 in numerals and in words
use place value and number facts to solve problems.
-count from 0 in multiples of 4, 8, 50 and 100; find 10 or 100 more or less than a given number
Divide 100 into 2, 4, 5 and 10 equal parts, and read scales/number lines marked in multiples of 100 with $2,4,5$ and 10 equal parts.
-recognise the place value of each digit in a three-digit number (hundreds, tens, ones)
-Recognise the place value of each digit in three-digit numbers, and compose and decompose three-digit numbers using standard and non-standard partitioning.
-Know that 10 tens are equivalent to 1 hundred, and that 100 is 10 times the size of 10 ; apply this to identify and work out how many 10s there are in other three digit multiples of 10. -compare and order numbers up to 1000 Reason about the location of any three digit number in the linear number system, including identifying the previous and next multiple of 100 and 10.

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-read, write and interpret mathematical statements involving addition (+), subtraction ( - ) and equals (=) signs
-represent and use number bonds and related subtraction facts within 20
-add and subtract one-digit and two-digit numbers to 20, including zero
-solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7=-9$.
-solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher
-Reason about the location of any two-digit number in the linear number system, including identifying the previous and next multiple of 10
-solve problems with addition and subtraction:

- using concrete objects and pictorial representations, including those involving numbers, quantities and measures
- applying their increasing knowledge of mental and written methods
-recall and use addition and subtraction facts to 20
fluently, and derive and use related facts up to 100
-Secure fluency in addition and subtraction facts within 10, through continued practice.
-add and subtract numbers using concrete objects,
pictorial representations, and mentally, including:
- a two-digit number and ones
- a two-digit number and tens
- two two-digit numbers
- adding three one-digit numbers
-show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot
-Add and subtract within 100 by applying related onedigit addition and subtraction facts: add and subtract only ones or only tens to/from a two digit number.
-recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.


## -Add and subtract across 10.

-Recognise the subtraction structure of 'difference' and answer questions of the form, "How many more...?".
-recall and use multiplication and division facts for the 2,5 and 10 multiplication tables, including recognising odd and even numbers
-calculate mathematical statements for multiplication and division within the multiplication tables and write them
using the multiplication $(\times)$, division ( $\div$ ) and equals ( $=$ ) signs -show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot
Relate grouping problems where the number of groups is unknown to multiplication equations with a missing factor, and to division equations (quotitive division).
-identify, represent and estimate numbers using different representations
-read and write numbers up to 1000 in numerals and in words -solve number problems and practical problems involving these ideas.
-add and subtract numbers mentally, including:

- a three-digit number and ones
- a three-digit number and tens
- a three-digit number and hundreds
-add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction -estimate the answer to a calculation and use inverse operations to check answers
Secure fluency in addition and subtraction facts that bridge 10, through continued practice.
-solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction.
-Apply place-value knowledge to known additive and multiplicative number facts (scaling facts by 10). -Manipulate the additive relationship: Understand the inverse relationship between addition and subtraction, and how both relate to the part-part-whole structure.
-Understand and use the commutative property of addition, and understand the related property for subtraction.
-recall and use multiplication and division facts for the 3,4 and 8 multiplication tables
Recall multiplication facts, and corresponding division facts, in the 10, 5, 2, 4 and 8 multiplication tables, and recognise products in these multiplication tables as multiples of the corresponding number.
-write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods -Apply known multiplication and division facts to solve contextual problems with different structures, including quotitive and partitive division.
-solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which $n$ objects are connected to m objects.


|  | -sequence events in chronological order using language [for example, before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] <br> -recognise and use language relating to dates, including days of the week, weeks, months and years <br> -tell the time to the hour and half past the hour and draw the hands on a clock face to show these times. |  |  |
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| Geometry | -recognise and name common 2-D and 3-D shapes, including: <br> - 2-D shapes [for example, rectangles (including squares), circles and triangles] <br> - 3-D shapes [for example, cuboids (including cubes), pyramids and spheres]. -describe position, direction and movement, including whole, half, quarter and three-quarter turns. | -identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line <br> -identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces -identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid] -compare and sort common 2-D and 3-D shapes and everyday objects. <br> Use precise language to describe the properties of 2D and 3D shapes, and compare shapes by reasoning about similarities and differences in properties. <br> -order and arrange combinations of mathematical objects in patterns and sequences -use mathematical vocabulary to describe position, direction and movement, including movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anticlockwise). | -draw 2-D shapes (Draw polygons by joining marked points) and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them -recognise angles as a property of shape or a description of a turn -identify right angles of shapes in different orientations, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle -identify horizontal and vertical lines and pairs of perpendicular and parallel lines. |
| Statistics |  | -interpret and construct simple pictograms, tally charts, block diagrams and simple tables <br> -ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity <br> -ask and answer questions about totalling and comparing categorical data. | -interpret and present data using bar charts, pictograms and tables <br> -solve one-step and two-step questions [for example, ‘How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables. |
| Ratio and Proportion |  |  |  |

## Upper Phase

|  | Year 4 | Year 5 | Year 6 |
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| Number - Place Value | -count in multiples of $6,7,9,25$ and 1000 <br> -find 1000 more or less than a given number - Know that 10 hundreds are equivalent to 1 thousand, and that 1,000 is 10 times the size of $\mathbf{1 0 0}$; apply this to identify and work out how many 100s there are in other four-digit multiples of 100 . <br> -count backwards through zero to include negative numbers <br> -recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) <br> -order and compare numbers beyond 1000 <br> -identify, represent and estimate numbers using different representations -compose and decompose four-digit numbers using standard and nonstandard partitioning. <br> -round any number to the nearest 10, 100 or 1000 and reason about its location -solve number and practical problems that involve all of the above and with increasingly large positive numbers <br> -read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value. | -read, write, order and compare numbers to at least 1000 000 and determine the value of each digit <br> -count forwards or backwards in steps of powers of 10 for any given number up to 1000000 <br> -interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero <br> -round any number up to 1000000 to the nearest 10,100 , 1000, 10000 and 100000 <br> -solve number problems and practical problems that involve all of the above <br> -read Roman numerals to 1000 (M) and recognise years written in Roman numerals. | -read, write, order and compare numbers up to 10000000 and determine the value of each digit <br> -round any whole number to a required degree of accuracy <br> -use negative numbers in context, and calculate intervals across zero <br> -solve number and practical problems that involve all of the above. |


|  | Divide 1,000 into 2, 4, 5 and 10 equal parts, and read scales/number lines marked in multiples of 1,000 with 2 , 4,5 and 10 equal parts. |  |  |
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| Number (add, subtract, multiply and divide) | -add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate <br> -estimate and use inverse operations to check answers to a calculation <br> -solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why <br> -recall multiplication and division facts for multiplication tables up to $12 \times 12$ and recognise products in multiplication tables as multiples of the corresponding number. <br> -use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1 ; dividing by 1 ; multiplying together three numbers <br> -recognise and use factor pairs and commutativity in mental calculations <br> Understand and apply the distributive property of multiplication <br> -multiply two-digit and three-digit numbers by a one-digit number using formal written layout <br> -Multiply and divide whole numbers by 10 and 100 (keeping to whole number quotients); understand this as equivalent to making a number 10 or 100 times the size. <br> -solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects. | -add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) <br> -add and subtract numbers mentally with increasingly large numbers <br> -use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy <br> -solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why. <br> -identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers <br> -know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers <br> -establish whether a number up to 100 is prime and recall prime numbers up to 19 <br> -multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers <br> -multiply and divide numbers mentally drawing upon known facts <br> -divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context <br> -multiply and divide whole numbers and those involving decimals by 10,100 and 1000 <br> -recognise and use square numbers and cube numbers, and the notation for squared ( 2 ) and cubed (3) | -multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication <br> -divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context <br> -divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context <br> -perform mental calculations, including with mixed operations and large numbers <br> -identify common factors, common multiples and prime numbers <br> -use their knowledge of the order of operations to carry out calculations involving the four operations <br> -solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why <br> -solve problems involving addition, subtraction, multiplication and division <br> -use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy. |


|  | -Solve division problems, with two-digit dividends and one-digit divisors, that involve remainders, and interpret remainders appropriately according to the context. | -solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes <br> -solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign <br> -solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates. |  |
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| Number (Fractions including decimals and percentages) | -Reason about the location of mixed numbers in the linear number system. <br> -recognise and show, using diagrams, families of common equivalent fractions <br> -count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten. <br> -solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number <br> -Convert mixed numbers to improper fractions and vice versa. <br> -add and subtract fractions with the same denominator <br> -recognise and write decimal equivalents of any number of tenths or hundredths <br> -recognise and write decimal equivalents to $41,21,43$ <br> -find the effect of dividing a one- or two-digit number by 10 and 100 , identifying the value of the digits in the answer as ones, tenths and hundredths <br> -round decimals with one decimal place to the nearest whole number <br> -compare numbers with the same number of decimal places up to two decimal places | -compare and order fractions whose denominators are all multiples of the same number <br> -identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths <br> -recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements $>1$ as a mixed number [for example, $52+54=56=151$ ] <br> -add and subtract fractions with the same denominator and denominators that are multiples of the same number <br> -multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams -read and write decimal numbers as fractions [for example, $0.71=$ 10071 ] <br> -recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents <br> -round decimals with two decimal places to the nearest whole number and to one decimal place <br> -read, write, order and compare numbers with up to three decimal places <br> -solve problems involving number up to three decimal places <br> -recognise the per cent symbol (\%) and understand that per cent relates to 'number of parts per hundred', and | -use common factors to simplify fractions; use common multiples to express fractions in the same denomination compare and order fractions, including fractions > 1 <br> -add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions <br> -multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, $41 \times 21=81$ ] <br> -divide proper fractions by whole numbers [for example, 3 $1 \div 2=61$ ] -associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, 83] <br> -identify the value of each digit in numbers given to three decimal places and multiply and divide numbers by 10,100 and 1000 giving answers up to three decimal places multiply one-digit numbers with up to two decimal places by whole numbers <br> - use written division methods in cases where the answer has up to two decimal places <br> -solve problems which require answers to be rounded to specified degrees of accuracy -recall and use equivalences between simple fractions, decimals and percentages, including in different contexts. |


|  | -solve simple measure and money problems involving fractions and decimals to two decimal places. | write percentages as a fraction with denominator 100, and as a decimal <br> -solve problems which require knowing percentage and decimal equivalents of $21,41,51,52,54$ and those fractions with a denominator of a multiple of 10 or 25 |  |
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| Measurement | -Convert between different units of measure [for example, kilometre to metre; hour to minute] -measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres -find the area of rectilinear shapes by counting squares <br> -estimate, compare and calculate different measures, including money in pounds and pence <br> -read, write and convert time between analogue and digital 12- and 24-hour clocks <br> -solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days | -convert between different units of metric measure (for example, kilometre and metre; centimetre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre) <br> -understand and use approximate equivalences between metric units and common imperial units such as inches, pounds and pints <br> -measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres <br> -calculate and compare the area of rectangles (including squares), and including using standard units, square centimetres ( cm 2 ) and square metres ( m 2 ) and estimate the area of irregular shapes -estimate volume [for example, using 1 cm 3 blocks to build cuboids (including cubes)] and capacity [for example, using water] <br> -solve problems involving converting between units of time <br> -use all four operations to solve problems involving measure [for example, length, mass, volume, money] using decimal notation, including scaling. | -solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate <br> -use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimal places -convert between miles and kilometres <br> -recognise that shapes with the same areas can have different perimeters and vice versa <br> -recognise when it is possible to use formulae for area and volume of shapes <br> -calculate the area of parallelograms and triangles <br> -calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm3) |
| Geometry (properties of shape and position and direction) | -Identify regular polygons, including equilateral triangles and squares, as those in which the side-lengths are equal and the angles are equal. Find the perimeter of regular and irregular polygons. <br> -compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes <br> -identify acute and obtuse angles and compare and order angles up to two right angles by size | -identify 3-D shapes, including cubes and other cuboids, from 2-D representations <br> -know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles <br> -draw given angles, and measure them in degrees (o) identify: <br> - angles at a point and one whole turn (total 360o ) <br> - angles at a point on a straight line and 21 a turn (total 180o ) | -draw 2-D shapes using given dimensions and angles -recognise, describe and build simple 3-D shapes, including making nets <br> -compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons <br> -illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius |


|  | -identify lines of symmetry in 2-D shapes presented in different orientations <br> -complete a simple symmetric figure with respect to a specific line of symmetry. <br> -describe positions on a 2-D grid as coordinates in the first quadrant <br> -describe movements between positions as translations of a given unit to the left/right and up/down <br> -plot specified points and draw sides to complete a given polygon. <br> -Draw polygons, specified by coordinates in the first quadrant, and translate within the first quadrant. | - other multiples of 900 -use the properties of rectangles to deduce related facts and find missing lengths and angles <br> -distinguish between regular and irregular polygons based on reasoning about equal sides and angles. <br> -identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed. | -recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles. <br> -describe positions on the full coordinate grid (all four quadrants) <br> -draw and translate simple shapes on the coordinate plane, and reflect them in the axes. |
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| Statistics | -interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs. <br> -solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs. | -solve comparison, sum and difference problems using information presented in a line graph <br> -complete, read and interpret information in tables, including timetables. | -interpret and construct pie charts and line graphs and use these to solve problems -calculate and interpret the mean as an average. |
| Ratio and Proportion |  |  | solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts <br> -solve problems involving the calculation of percentages [for example, of measures, and such as $15 \%$ of 360 ] and the use of percentages for comparison <br> -solve problems involving similar shapes where the scale factor is known or can be found <br> -solve problems involving unequal sharing and grouping using knowledge of fractions and multiples. |
| Algebra |  |  | -use simple formulae -generate and describe linear number sequences -express missing number problems algebraically -find pairs of numbers that satisfy an equation with two unknowns -enumerate possibilities of combinations of two variables. |

